Theories of pseudopotentials

- 1. OPW method
- 2. PK type pseudopotential
- 3. Norm-conserving pseudopotential by TM
- 4. Ultra-soft pseudopotential by Vanderbilt
- 5. MBK pseudopotential
- 6. Solving the 1D Dirac eq.
- 7. What we can do if we generate PPs by ourselves
- 8. On the vps file

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The Summer School on DFT: Theories and Practical Aspects, July 2-6, 2018, ISSP

Intuitive ideas of pseudopotentials

- Since core electrons is situated at energetically very deeper states, they are inert chemically. In molecules and solids, they do not change so largely.
- 2. Is there a way of constructing an effective potential consisting of the nucleus potential and Coulomb potential given by the core electrons states calculated in advance ?
- 3. If the effective potential is much shallower than that of the true nucleus potential, it is expected that the calculation will become quite easier.



Electronic structure of Si bulk

Science **351**, aad3000 (2016).

OPW (Orthogonalized Plane Wave Method) method

C. Herring, Phys. Rev. 57, 1169 (1940)

$$\hat{H} \left| \psi_i \right\rangle = E_i \left| \psi_i \right\rangle \qquad i = \text{c,v}$$

It is assumed that $|\Psi_c\rangle$ has been solved in advance. $|PW, \mathbf{q}\rangle = \exp(i\mathbf{q}\cdot\mathbf{r})$ is orthogonalized with $|\Psi_c\rangle$ by

$$|OPW,\mathbf{q}\rangle = |PW,\mathbf{q}\rangle - \sum_{c} |\psi_{c}\rangle \langle \psi_{c}|PW,\mathbf{q}\rangle$$

It is easy to verify that

$$\langle \psi_{c'} | OPW, \mathbf{q} \rangle = \langle \psi_{c'} | PW, \mathbf{q} \rangle - \sum_{c} \langle \psi_{c'} | \psi_{c} \rangle \langle \psi_{c} | PW, \mathbf{q} \rangle$$
$$= \langle \psi_{c'} | PW, \mathbf{q} \rangle - \langle \psi_{c'} | PW, \mathbf{q} \rangle = 0$$

By using the OPW as basis set, the number of basis functions can be reduced



valence electrons oscillate near the vicinity of nucleus because of the orthogonality with core electrons.



Phillips-Kleinman (PK) method

Phys. Rev. 116, 287 (1959)

Smooth part of wave funtion Orthogonalize it with core electrons Let's write Eq. by $|\phi\rangle$

Let's write Eq. by
$$|\psi\rangle$$

L.H.S
 $\hat{H}|\Psi\rangle = \hat{H}|\phi\rangle - \sum_{c} \hat{H}|\psi_{c}\rangle\langle\psi_{c}|\phi\rangle$
 $\simeq \hat{H}|\phi\rangle - \sum_{c} E_{c}|\psi_{c}\rangle\langle\psi_{c}|\phi\rangle$

One can get by equating L.H.S with R.H.S.

 \hat{H}

$$\left(\hat{H} + \sum_{c} (E - E_{c}) |\psi_{c}\rangle \langle \psi_{c}|\right) |\phi\rangle = E |\phi\rangle$$

This gives a new view that $|\phi\rangle$ feels the following effective potential.

$$v_{\rm eff} = v_{\rm ext} + \sum_{\rm c} \left(\frac{E - E_{\rm c}}{Positive in general} \right) \left| \psi_{\rm c} \right\rangle \left\langle \psi_{\rm c} \right|$$

V_{eff} is shallower than v.

$$\begin{aligned} \left| \phi \right\rangle &= \sum_{\mathbf{G}} C_{\mathbf{G}} \left| PW, \mathbf{G} \right\rangle \\ \left| \Psi \right\rangle &= \left| \psi \right\rangle - \sum \left| \psi_{\mathbf{c}} \right\rangle \langle \psi_{\mathbf{c}} \left| \phi \right\rangle \\ \hat{H} \left| \Psi \right\rangle &= E \left| \Psi \right\rangle \end{aligned}$$

R.H.S

$$E\left|\Psi\right\rangle = E\left|\phi\right\rangle - \sum_{c} E\left|\psi_{c}\right\rangle\left\langle\psi_{c}\right|\phi\right\rangle$$

Features of V_{eff}

- 1. Non-local potential
- 2. Energy dependent
- 3. For a linear transformation

$$|\phi'\rangle = |\phi\rangle - \sum_{c} |\psi_{c}\rangle \langle \psi_{c} |\phi\rangle$$

the form of Eq. is invariant.

Scattering by a spherical potential



Norm-conserving pseudopotential by Troullier and Matins

N. Troullier and J. L. Martins, Phys. Rev. B 43, 1993 (1991).

$$\left[-\frac{1}{2}\frac{d^2}{dr^2} + \frac{l(l+1)}{2r^2} + V(r)\right]u_l(r) = \varepsilon_l u_l(r) \qquad R_l(r) = \frac{u_l(r)}{r}$$

For $u_l(r)$, the following form is used.

$$u_{l}(r) = \begin{cases} u_{l}^{(AE)}(r) & r \ge r_{cl} \\ r^{l+1} \exp[p(r)] & r \le r_{cl} \end{cases} \qquad p(r) = \sum_{i=0}^{6} c_{2i} r^{2i}$$

Putting u₁ into radial Schroedinger eq. and solving it with respect to V, we have

$$V^{(\text{scr})}(r) = \varepsilon_l - \frac{l(l+1)}{2r^2} + \frac{1}{2} \frac{u''_l(r)}{u_l(r)}$$

= $\varepsilon_l + \frac{l(l+1)p'(r)}{r} + \frac{1}{2} \left[p''(r) + [p'(r)]^2 \right]$

 $c_0 \sim c_{12}$ are determined by the following conditions:

- Norm-conserving condition within the cutoff radius
- The second derivatives of V $^{(scr)}$ is zero at r=0
- Equivalence of the derivatives up to 4^{th} orders of u_1 at the cutoff radius

Unscreeing and partial core correction (PCC)

Unscreeing

Since $V^{(scr)}$ contains effect of valence electrons, the ionic pseudopotential is constructed by subtracting the effects.

$$V_{l}^{(\text{ps})}(r) = V_{l}^{(\text{scr})}(r) - V_{\text{Hartree}}(r) - V_{\text{xc}}[\rho_{v}(r) + \rho_{\text{pcc}}(r)]$$



Partial Core Correction(PCC)

In order take account of the non-linearity of exchangecorrelation term, it would be better to include the partial core correction.

Pseudopotentials by the TM method

Red: All electron calculation Blue: Pseudopotential



Separable pseudopotentials

Since the pseudopotential depends on the angular momentum *l*, it is **non-local.**

$$V^{(\text{PS})}(\mathbf{r}) = V_{loc}(\mathbf{r},\mathbf{r}')\delta(\mathbf{r}-\mathbf{r}') + V_{\text{NL}}(\mathbf{r},\mathbf{r}')$$
$$V_{\text{NL}}(\mathbf{r},\mathbf{r}') = \sum_{lm} |Y_l^m(\hat{\mathbf{r}})\rangle \langle V_l^{(\text{PS})}(r) - V_{loc}(r)\rangle \langle Y_l^m(\hat{\mathbf{r}})|$$
$$= \sum_{lm} |Y_l^m(\hat{\mathbf{r}})\rangle V_l^{(\text{NL})}(r) \langle Y_l^m(\hat{\mathbf{r}})|$$
$$= \sum_{lm} \sum_{\zeta} |V_l^{(\text{NL})}\overline{R}_{l\zeta}Y_l^m\rangle \frac{1}{c_{l\zeta}} \langle Y_l^m\overline{R}_{l\zeta}V_l^{(\text{NL})}|$$

The non-local potential is usually used as a separable form due to the simplicity of calculations.

L Kleinman and D. M. Bylander, PRL 48, 1425 (1982).

P. E. Blöchl, Phys. Rev. B 41, 5414 (1990).

Ultrasoft pseudopotential by Vanderbilt

D. Vanderbilt, PRB 41, 7892 (1990).

The phase shift is reproduced around multiple reference energies by the following non-local operator.

$$V_{\rm NL} = \sum_{i,j} B_{ij} |\beta_i\rangle \langle\beta_j|$$

$$|\chi_i\rangle = V_{\rm NL}^{(i)} |\phi_i\rangle = (\varepsilon_i - T - V_{\rm loc}) |\phi_i\rangle$$
$$B_{ij} = \langle \phi_i |\chi_j\rangle$$

$$|\beta_i\rangle = \sum_j (B^{-1})_{ji} |\chi_j\rangle$$

If the following generalized norm conserving condition is fulfilled, the matrix B is Hermitian. Thus, in the case the operator V_{NL} is also Hermitian.

$$Q_{ij} = \langle \psi_i | \psi_j \rangle_R - \langle \phi_i | \phi_j \rangle_R$$
$$B_{ij} - B_{ji}^* = (\varepsilon_i - \varepsilon_j) Q_{ij}$$

If Q=0, then $B-B^*=0$

How the non-local operator works?

Operation of the non-local operator to pseudized wave function

$$\begin{split} \hat{v}^{(\mathrm{NL})} |\phi_{k}^{(\mathrm{PS})}\rangle &= \sum_{ij} |\beta_{i}\rangle B_{ij} \langle\beta_{j}|\phi_{k}^{(\mathrm{PS})}\rangle \\ &= \sum_{ij} |\beta_{i}\rangle B_{ij} \sum_{k'} (B^{-1})_{k'j} \langle\chi_{k'}|\phi_{k}^{(\mathrm{PS})}\rangle, \\ &= \sum_{ij} |\beta_{i}\rangle B_{ij} \sum_{k'} (B^{-1})_{k'j} B_{kk'}, \\ &= \sum_{ij} |\beta_{i}\rangle B_{ij} \delta_{kj}, \\ &= \sum_{ij} |\beta_{i}\rangle B_{ij} \delta_{kj}, \\ &= \sum_{ij} |\beta_{i}\rangle B_{ij} \delta_{kj}, \\ &= \sum_{ij} |\beta_{i}\rangle B_{ij} \langle\chi_{j}\rangle B_{ik}. \\ &= |\chi_{k}\rangle \end{split}$$
Note that
$$\begin{aligned} &\text{Note that} \\ v^{(\mathrm{SL})}(r) &= v_{\mathrm{L}}(r) + v_{\mathrm{H}}^{(\mathrm{v})}(r) + v_{\mathrm{xc}}^{(\mathrm{v}+\mathrm{pcc})}(r). \\ &|\chi_{i}\rangle &= (\varepsilon_{i} + \frac{1}{2}\nabla^{2} - v^{(\mathrm{SL})}(r)) |\phi_{i}^{(\mathrm{PS})}\rangle, \\ &= \sum_{ij} |\beta_{i}\rangle B_{ij} \langle\chi_{j}\rangle B_{ik}. \\ &= |\chi_{k}\rangle \end{aligned}$$

It turns out that the following Schroedinger equation is satisfied.

$$\left(-\frac{1}{2}\nabla^2 + v^{(\mathrm{SL})}(r) + \hat{v}^{(\mathrm{NL})}\right) |\phi_i^{(\mathrm{PS})}\rangle = \varepsilon_i |\phi_i^{(\mathrm{PS})}\rangle.$$

The matrix B and the generalized norm conserving condition

The matrix B is given by

$$B_{ij} = \int_0^{r_c} dr P_i^{(PS)}(r) \left(\varepsilon_j + \frac{1}{2} \frac{d^2}{dr^2} - \frac{l(l+1)}{2r^2} - v^{(SL)}(r) \right) P_j^{(PS)}(r),$$

$$B_{ji}^* = \int_0^{r_c} dr P_i^{(PS)}(r) \left(\varepsilon_i + \frac{1}{2} \frac{d^2}{dr^2} - \frac{l(l+1)}{2r^2} - v^{(SL)}(r) \right) P_j^{(PS)}(r),$$

Thus, we have

$$B_{ij} - B_{ji}^* = (\varepsilon_j - \varepsilon_i) \int_0^{r_c} dr P_i^{(PS)}(r) P_j^{(PS)}(r) + \frac{1}{2} \int_0^{r_c} dr P_i^{(PS)}(r) P_j^{\prime\prime(PS)}(r) - \frac{1}{2} \int_0^{r_c} dr P_i^{\prime\prime(PS)}(r) P_j^{(PS)}(r).$$

- 00

By integrating by parts

$$B_{ij} - B_{ji}^{*} = (\varepsilon_{j} - \varepsilon_{i}) \langle \phi_{i}^{(\text{PS})} | \phi_{j}^{(\text{PS})} \rangle_{r_{c}} + \frac{1}{2} \left[P_{i}^{(\text{PS})}(r) P_{j}^{\prime(\text{PS})}(r) \right]_{0}^{r_{c}} - \frac{1}{2} \left[P_{i}^{\prime(\text{PS})}(r) P_{j}^{(\text{PS})}(r) \right]_{0}^{r_{c}},$$

$$= (\varepsilon_{j} - \varepsilon_{i}) \langle \phi_{i}^{(\text{PS})} | \phi_{j}^{(\text{PS})} \rangle_{r_{c}} + \frac{1}{2} P_{i}^{(\text{PS})}(r_{c}) P_{j}^{\prime(\text{PS})}(r_{c}) - \frac{1}{2} P_{i}^{\prime(\text{PS})}(r_{c}) P_{j}^{(\text{PS})}(r_{c}). \quad \cdots \quad (1)$$

By performing the similar calculations, we obtain for the all electron wave functions

$$0 = (\varepsilon_j - \varepsilon_i) \langle \phi_i^{(AE)} | \phi_j^{(AE)} \rangle_{r_c} + \frac{1}{2} P_i^{(AE)}(r_c) P_j^{\prime(AE)}(r_c) - \frac{1}{2} P_i^{\prime(AE)}(r_c) P_j^{(AE)}(r_c).$$
(2)

By subtracting (2) from (1), we have the following relation.

$$B_{ij} - B_{ji}^* = (\varepsilon_i - \varepsilon_j) \left(\langle \phi_i^{(AE)} | \phi_j^{(AE)} \rangle_{r_c} - \langle \phi_i^{(PS)} | \phi_j^{(PS)} \rangle_{r_c} \right).$$

Norm-conserving pseudopotential by MBK

I. Morrion, D.M. Bylander, and L. Kleinman, PRB 47, 6728 (1993).

If $Q_{ij} = 0$, the non-local operator can be transformed to a diagonal form.

$$V_{\rm NL} = \sum_{i,j} B_{ij} |\beta_i\rangle \langle\beta_j|,$$
$$= \sum_i \lambda_i |\alpha_i\rangle \langle\alpha_i|$$

The form is exactly the same as that for the Blöchl expansion, resulting in no need for modification of OpenMX.

To satisfy $Q_{ij}=0$, the pseudized wave function is written by

$$\phi_i = \phi_{\mathrm{TM},i} + f_i \quad f_i = \sum_{i=0} c_i \left[r j_l \left(\frac{r}{r_c} u_{li} \right) \right]$$

The coefficients can be determined by matching up to the third derivatives to those for the all electron, and $Q_{ij}=0$. Once *c*'s are determined, χ is given by

$$\chi_i = V_{\rm TM}^{(i)} \phi_{\rm TM,i} + \varepsilon_i f_i - V_{\rm loc} \phi_i - \frac{1}{2} \sum_i c_i \left(\frac{u_{li}}{r_c}\right)^2 \left[r j_l \left(\frac{r}{r_c} u_{li}\right)\right]$$

The form of MBK pseudopotentials

The pseudopotential is given by the sum of a local term V_{loc} and non-local term V_{NL} .

$$V^{(\rm ps)} = V_{\rm loc}(r) + V_{\rm NL}$$

The local term V_{loc} is independent of the angular channel *l*. On the other hand, the non-local term V_{NL} is given by projectors

$$V_{\rm NL} = \sum_{i} \lambda_i \mid \alpha_i \rangle \langle \alpha_i \mid$$

The projector consists of radial and spherical parts, and depends on atomic species, energy-channel, and l-channel.

Relativistic pseudopotentials

By using the eigenfunctions of the spherical operator for the Dirac Eq., one can introduce a relativistic pseudopotential as

$$\begin{split} V^{(\text{ps})} &= v^{(\text{L})} + \sum_{lm} \left[|\Phi_J^M \rangle v_{l+\frac{1}{2}}^{(\text{NL})} \langle \Phi_J^M | + |\Phi_{J'}^{M'} \rangle v_{l-\frac{1}{2}}^{(\text{NL})} \langle \Phi_{J'}^{M'} | \right] \\ &= v^{(\text{L})} + \hat{v}_{l+\frac{1}{2}}^{(\text{NL})} + \hat{v}_{l-\frac{1}{2}}^{(\text{NL})}, \end{split}$$

for $J = l + \frac{1}{2}$ and $M = m + \frac{1}{2}$

$$|\Phi_J^M\rangle = \left(\frac{l+m+1}{2l+1}\right)^{\frac{1}{2}} |Y_l^m\rangle |\alpha\rangle + \left(\frac{l-m}{2l+1}\right)^{\frac{1}{2}} |Y_l^{m+1}\rangle |\beta\rangle,$$

for $J' = l - \frac{1}{2}$ and $M' = m - \frac{1}{2}$ $|\Phi_{J'}^{M'}\rangle = \left(\frac{l-m+1}{2l+1}\right)^{\frac{1}{2}} |Y_l^{m-1}\rangle |\alpha\rangle - \left(\frac{l+m}{2l+1}\right)^{\frac{1}{2}} |Y_l^m\rangle |\beta\rangle.$

Optimization of pseudopotentials



Comparison of logarithmic derivatives

Logarithmic derivatives of wave functions for s, p, d, and f channels for Mn atom. It is found that the separable MBK is well compared with the all-electron. If there is a deviation in the logarithmic derivatives, the band structure will not be reproduced.



OpenMX vs. Wien2k in fcc Mn



1D-Dirac equation with a spherical potential

1-dimensional radial Dirac equation for the majority component G is given by

$$\left[\frac{1}{2m_{nlj}(r)}\left(\frac{d^2}{dr^2} + \frac{\alpha^2}{2m_{nlj}(r)}\frac{dv_{\text{eff}}}{dr}\frac{d}{dr} + \frac{\alpha^2}{2m_{nlj}(r)}\frac{\kappa}{r}\frac{dv_{\text{eff}}}{dr} - \frac{\kappa(\kappa+1)}{r^2}\right) + \varepsilon_{nlj} - v_{\text{eff}}\right]G_{nlj} = 0,$$

The mass term is given by

$$m_{nlj}(r) = 1 + \frac{\alpha^2(\varepsilon_{nlj} - v_{\text{eff}})}{2}$$
.
Minority component
 $F_{nlj} = \frac{\left(\frac{d}{dr} + \frac{\kappa}{r}\right)G_{nlj}}{\alpha\left[\frac{2}{a^2} + \varepsilon_{nlj} - v_{\text{eff}}(r)\right]F_{nlj}}$.

By expressing the function G by the following form,

$$G_{nlj}(r) = r^{l+1} L_{nlj}(r).$$

One obtain a set of equations:

$$\frac{dL_{nlj}}{dx} = M_{nlj},$$

$$\frac{dM_{nlj}}{dx} = -(2l+1+\frac{r\alpha^2}{2m_{nlj}}\frac{dv_{\text{eff}}}{dr})M_{nlj} - \frac{r\alpha^2}{2m_{nlj}}\frac{dv_{\text{eff}}}{dr}(l+1+\kappa)L_{nlj} + 2m_{nlj}r^2(v_{\text{eff}}-\varepsilon_{nlj})L_{nlj}.$$

The charge density is obtained from

$$\rho(r) = \sum_{n,l,j} q_{nlj} \frac{G_{nlj}(r)^2 + F_{nlj}(r)^2}{4\pi r^2},$$

Solving the 1D-Dirac equation

By changing the variable r to x with $r = e^x$, and applying a predictor and corrector method, we can derive the following equations:

$$L_{i+1}^{(p)} = 32L_i - 31L_{i-1} - dx(16M_i + 14M_{i-1}) + dx^2(4M'_i - 2M'_{i-1}),$$

$$M_{i+1}^{(p)} = -4M_i + 5M_{i-1} + dx(4M'_i + 2M'_{i-1}),$$

$$M_{i+1}^{(c)} = M_i + \frac{dx}{12}(8M'_i - M'_{i-1} + 5M'^{(p)}_{i+1}),$$

$$L_{i+1}^{(c)} = L_i + \frac{dx}{12}(8M_i - M_{i-1} + 5M^{(c)}_{i+1}).$$
For a given E, the L and M are solved from the origin and distant region, and they are matched at a matching point.

1

4000 4000 "sol_o" u 2:3 "sol 0" u 2:4 "sol_i" u 2:(76000*\$3) "sol_i" u 2:(76000*\$4) 3500 3000 3000 2000 2500 Μ 2000 1000 L 1500 1000 -1000 500 -2000 0,0001 1 10 0,001 0.01 0.1 100 0,0001 0.001 0.01 0.1 1 10 100 r (a.u.) r (a.u.)

origin and

In All_Electron.c, the calculation is performed.

How to find eigenstates #1

If the chosen E is an eigenvalue, the following Eq. is hold:

$$\frac{L_O(r_{\rm MP})}{L_I(r_{\rm MP})} = \frac{M_O(r_{\rm MP})}{M_I(r_{\rm MP})}$$

 r_{MP} is the radius corresponding to the matching point.

So, if ΔD is zero, it turns out that the chosen E is the eigenvalue.

$$\Delta D = M_O(r_{\rm MP}) - \alpha M_I(r_{\rm MP})$$

$$\alpha = \frac{L_O(r_{\rm MP})}{L_I(r_{\rm MP})}$$

In the right figure ΔD is plotted as a function of E for a hydrogen atom.

Since the analytic solution for a hydrogen atom is known,

$$E=-\frac{1}{2}\frac{Z^2}{n^2}$$

we can confirm that the zeros of ΔD correspond to the analytic eigenvalues.



How to find eigenstates #2

The sign of ΔD varies at an eigenvalue.

Algorithm of searching an eigenvalue E

(1) Look for the regime where ∆D changes the sign by scanning energy.
(2) The regime is narrowed by a bisection method.

(3) Once a convergence criterion is fulfilled, an eigenvalue is found

What we can do if we generate PPs by ourselves

It might be true that generating a good PP requires experiences more or less. So, it would be better for beginners to use a well-tested database of PPs. However, if you can generate PPs by yourself, you may be able to explore physics and chemistry by controlling PPs as parameters in a model theory. For example, the following calculations becomes possible.

1. Calculations of core-level binding energies

In order to calculate core-level binding energies measured by XPS, we need to generate PPs including the targeted core states.

2. Impurity problem using a virtual atom

PPs having non-integer valence electrons can be used to study effects of dilute impurity.

3. Mixing of PPs for different elements

It is not easy to identify how the character of elements affects to properties of interest. By using a mixed PPs for different elements, there is a possibility that one finds how the physical property is governed by a specific character of elements.

Calculations of core-level binding energies

It is possible to calculate absolute binding energies of core levels in molecules and solids. To do that we have to generate a proper PP including the targeted state.

It is also important to develop the database of PPs including core states which are well studied in experiments.

buckled-like

t-Si

Zr

В



C.-C. Lee et al., Phys. Rev. B 95, 115437 (2017).

Impurity problem by a virtual atom

One of carbon atoms in the diamond unit cell including 8 carbon atoms is replaced by a virtual atom having 4.2 valence electrons. The calculation corresponds to $C_{7.8}N_{0.2}(=C_{39}N_1)$. Below is the DOS.



Diamond vs. Graphene



Diamond vs. Graphene from C to Si



Pseudopotential generator: ADPACK

Welcome to OpenMX Open source package for Material eXplorer

Contents

What's new

International Summer Workshop for July 2nd-12th, 2018 Patch (Ver. 3.8.5) to OpenMX Ver. 3.8 (June 12, 2018)

The pseudopotential generator for OpenMX · Download is available here.

- What is OpenMX?
- Manual of Ver. 3.8 Manual of Ver. 3.7
- Technical Notes
- Video Lectures
- Publications
- OpenMX Forum
- OpenMX Viewer
- Workshop
- Database of VPS and PAO
 - Ver. 2013
- ADPACK
- Miscellaneous informations
- Contributors
- Acknowledgment
- Opening positions
- Links

http://www.openmx-square.org/

What is ADPACK?

ADPACK (Atomic Density functional program PACKage) is a software to perform density functional calculations for a single atom

The features are listed below:

- All electron calculation by the Schrödinger or Dirac equation
- LDA and GGA treatment to exchange-correlation energy
- Finite element method (FEM) for the Schrödinger equation
- Pseudopotential generation by the TM, BHS, MBK schemes
- Pseudopotential generation for unbound states by Hamann's scheme
- Kleinman and Bylander (KB) separable pseudopotential
- Separable pseudopotential with Blöchl multiple projectors
- Partial core correction to exchange-correlation energy
- Logarithmic derivatives of wave functions
- Detection of ghost states in separable pseudopotentials
- Scalar relativistic treatment
- Fully relativistic treatment with spin-orbit coupling
- Generation of pseudo-atomic orbitals under a confinement potential

The pseudopotentials and pseudo-atomic orbitals can be the input data for OpenMX.

Programs of ADPACK

Programs:65 C rounties and 5 header files (50,000 lines)Link:LAPACK and BLAS

Main routine: adpack.c

Input: readfile.c, Inputtool.c

Output: Output.c

All electron calculations: All_Electron.c, Initial_Density.c, Core.c

Numerical solutions for Schroedinger and Dirac eqs.: Hamming_I.c, Hamming_O.c Density: Density.c, Density_PCC.c, Density_V.c

Exchange-Correlation: XC_CA.c, XC_EX.c, XC_PW91.c, XC_VWN.c, XC_PBE.c

Mixing: Simple_Mixing.c

Pseudopotentials: MBK.c, BHS.c, TM.c

Pseudo-atomic orbitals: Multiple_PAO.c

The global variables are declared in adpack.h.

Database (2013)

Database (2013) of optimized VPS and PAO



http://www.openmx-square.org/

Input file

File Name

System.CurrrentDir # default=./ ./ Pt_PBE13 System Name # ON OFF Log.print # NO|YES, default=NO # default=null System.UseRestartfile yes System.Restartfile Pt PBE13 ### Calculation type # sch|sdirac|dirac # ALL|VPS|PAO # LDA|GGA eq.type dirac calc.type vps GGA xc.type ### Atom AtomSpecies 78 6 max.occupied.N total .electron 78.0 valence.electron 16.0 <occupied.electrons 2.0 23 2.0 6.0 2.0 6.0 10.0 4 10.0 14.0 2.0 6.0 5 2.0 6.0 9.0 0.0 0.0 6 0.0 0.0 1.0 0.0 0.0 0.0 occupied.electrons>

In the header part, the input file for the ADPACK calculations are shown, which maybe helpful for the next generation of pseudopotentials.

Eigenvalues for all electron calculation

				j=1+1/2	j=l-1/2
n=	1	=	0	-2868.8969439503935	-2868.8969439503935
n=	2	=	0	-503.1142921617339	-503.1142921617339
n=	2	=	1	-419.1546670411121	-482.3720670651586
n=	3	=	0	-118.0771871048129	-118.0771871048129
n=	3	=	1	-94.8406495857986	-108.7310226714485
n=	3	=	2	-76.1768324508852	-79.1659107610239
n=	4	=	0	-25.3345514773071	-25.3345514773071
n=	4	=	1	-18.0570286040002	-21.3625609002204
n=	4	=	2	-10.9124371484223	-11.5257406345024
n=	4	=	3	-2.4568191349790	-2.5821360560534
n=	5	=	0	-3.6982650446879	-3.6982650446879
n=	5	=	1	-1.8910921655761	-2.4338351652662
n=	5	=	2	-0.2019516934267	-0.2496588022815
n=	6	=	0	-0.2079456213222	-0.2079456213222

The eigenvalues with $j=1\pm 1/2$ for the all electron calculations by the Dirac equation are included, which can be used to estimate the splitting by spin-orbit coupling

Information for pseudopotentials

vps.t	MBK						
numbe	5						
<pseudo.nandl< td=""></pseudo.nandl<>							
0	5	1	1.1000	0.0			
1	5	2	1.7000	0.0			
2	6	0	2.0000	0.0			
3	6	1	2.8000	0.0			
4	7	0	2.9000	-0.1			
pseudo.NandL>							

The specification for the pseudopotentials is made by vps.type, number.vps, and pseudo.NandL.

The project energies λ is shown as follows:

<project.energies< pre=""></project.energies<>								
7								
0	1.000000000000000e+00	1.000000000000000e+00						
0	1.000000000000000e+00	1.000000000000000e+00						
1	-1.000000000000000e+00	-1.000000000000000e+00						
1	-1.000000000000000e+00	-1.000000000000000e+00						
2	-1.000000000000000e+00	-1.000000000000000e+00						
2	-1.000000000000000e+00	-1.000000000000000e+00						
2	-1.000000000000000e+00	-1.000000000000000e+00						
proj	ect.energies>							

The generated pseudopotentials are output by Pseudo.Potentials

<Pseudo.Potentials 4.53999297624849e-05 -1.56274493573701e+01 -1.00000000000000e+01 1.29016191735297e+00 -3.53576793162279e-04 -2.74501529071506e-04 -2.44604572903325e-08 4.46045901596636e-08 5.09718887954710e-08 -9.97354909819639e+00 4.66168218439265e-05 -1.56274493573701e+01 1.29016191758754e+00 -3.63054006042743e-04 -2.81859221925009e-04 -2.57892987562848e-08 4.70277839806157e-08 5.37409931750746e-08 -9.94709819639279e+00 4.78663312960476e-05 -1.56274493573701e+01 -3.72785244541990e-04 -2.89414129143262e-04 1.29016191783448e+00 -2.71903310082123e-08 4.95826204925540e-08 5.66605322202532e-08 -9.92064729458918e+00 4.91493323893655e-05 -1.56274493573701e+01 1.29016191809451e+00 -3.82777317519879e-04 -2.97171536827178e-04 -2.86674758905822e-08 5.22762513305807e-08 5.97386784609548e-08 -9.89419639278557e+00 5.04667228281981e-05 -1.56274493573701e+01 1.29016191836861e+00 -3.93037216339845e-04 -3.05136872765505e-04 5.51162166502627e-08 6.29840484088342e-08 -3.02248683064018e-08 -9.86774549098196e+00 5.18194243787784e-05 -1.56274493573701e+01 1.29016191865760e+00 -4.03572119760603e-04 -3.13315710232509e-04

1st column: x

 2^{nd} column: r=exp(x) in a.u.

3rd column: radial part of local pseudopotential

4th and later columns: radial part of non-local pseudopotentials.

Charge density for partial core correction

<density.PCC</pre> -1.0000000000000e+01 4.53999297624849e-05 6.84116077628136e-01 -9.97354909819639e+00 4.66168218439265e-05 6.84116077628136e-01 -9.94709819639279e+00 4.78663312960476e-05 6.84116077628136e-01 -9.92064729458918e+00 4.91493323893655e-05 6.84116077628136e-01 -9.89419639278557e+00 5.04667228281981e-05 6.84116077628136e-01 -9.86774549098196e+00 5.18194243787784e-05 6.84116077628136e-01 -9.84129458917836e+00 5.32083835142066e-05 6.84116077628136e-01 6.84116077628136e-01 -9.81484368737475e+00 5.46345720766889e-05 6.84116077628136e-01 -9.78839278557114e+00 5.60989879575261e-05 -9.76194188376754e+00 5.76026557953301e-05 6.84116077628136e-01 -9.73549098196393e+00 5.91466276929535e-05 6.84116077628136e-01 -9.70904008016032e+00 6.07319839536367e-05 6.84116077628136e-01 -9.68258917835671e+00 6.23598338368870e-05 6.84116077628136e-01 _0_85813897855311₀±00_8_40313183348189₀_05 Q 9/110077099190a_01

> 1st column: x 2nd column: r=exp(x) in a.u. 3rd column: charge density for PCC

Outlook

- Although the development of PPs has a long history, and nowadays databases containing high-quality PPs are available.
 So, it would be better for beginners to use the well-tested database.
- Nevertheless it is important to understand the theories of PPs since this is a basis of current state-of-the-art technology in first-principles calculations.
- Actually, OpenMX is based on norm-conserving pseudopotentials developed by Morrison, Bylander, and Kleinman, PRB 47, 6728 (1993).
- If you can generate PPs by yourself, you may be able to explore physics and chemistry by controlling PPs as parameters in a model theory.